

Name:
Enrolment No:



UNIVERSITY OF PETROLEUM AND ENERGY STUDIES
End Semester Examination, December 2018

Programme Name: B.Tech. ECE+EE
Course Name : MATHEMATICS – I
Course Code : MATH – 1009
Nos. of page(s) : 02

Semester : I
Time : 03 hours
Max. Marks : 100

SECTION A

S. No.		Marks	CO
Q1	Find the Eigen values of $5A, 3A^3, 2A^{-1}, \frac{A}{3}$ if $A = \begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$.	4	CO1
Q2	Determine the Rank of the matrix $\begin{bmatrix} 1 & 2 & 3 \\ 1 & 4 & 2 \\ 2 & 6 & 5 \end{bmatrix}$.	4	CO1
Q3	Evaluate $\int_0^1 \int_0^x (x^2 + y^2) dA$, where dA indicates small area in xy -plane.	4	CO3
Q4	Find the Fourier coefficient a_n for $f(x) = x \sin x, 0 < x < 2\pi$	4	CO4
Q5	Prove $a_n = \frac{1}{\pi} \int_0^{2\pi} f(x) \cdot \cos nx \, dx$.	4	CO4

SECTION B

Q6	Find the inverse of matrix $\begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix}$ using Cayley Hamilton Theorem, also convert the expression $A^8 - 5A^7 + 7A^6 - 3A^5 + A^4 - 5A^3 + 8A^2 - 2A + I$ into quadratic equation.	8	CO1
Q7	Change the order of integration $\int_0^1 \int_{x^2}^{2-x} xy \, dy \, dx$ and hence evaluate.	8	CO3
Q8	Evaluate $\iint_R (x+y)^2 \, dx \, dy$, where R is the parallelogram in xy plane with vertices	8	CO3

	$(1, 0), (3, 1), (2, 2), (0, 1)$ using the transformation $u = x + y$ and $v = x - 2y$.		
Q9	Find the mass of tetrahedron bounded by coordinate axis and the plane $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ the variable density is $\rho = xyz$.	8	CO3
Q10	If $y_1 = \frac{x_2 x_3}{x_1}, y_2 = \frac{x_3 x_1}{x_2} \wedge y_3 = \frac{x_1 x_2}{x_3}$, find the Jacobean of x_1, x_2, x_3 wrt y_1, y_2, y_3 .	8	CO2
SECTION-C			
Q11 (A)	Prove that $\int_0^1 \frac{x^2 dx}{\sqrt{1-x^4}} \cdot \int_0^1 \frac{dx}{\sqrt{1+x^4}} = \frac{\pi}{4\sqrt{2}}$	10	CO2
Q11 (B)	If $f(x) = \begin{cases} 0, & -\pi \leq x \leq 0 \\ \sin x, & 0 < x \leq \pi \end{cases}$, Hence deduce the series $\frac{1}{1.3} - \frac{1}{3.5} + \frac{1}{5.7} - \dots = \frac{1}{4}(\pi - 2)$.	10	CO4
Q12 (A)	Show that the surface $x^2 - 2yz + y^3 = 4$ is perpendicular to any number of the family of surfaces $x^2 + 1 = (2 - 4a)y^2 + az^2$ at the point of intersection $(1, -1, 2)$	10	CO2
OR			
Q12 (A)	If $z = f(x, y)$ and $x = e^u \cos v, y = e^u \sin v$ prove that $x \frac{\partial z}{\partial v} + y \frac{\partial z}{\partial u} = e^{2u} \frac{\partial z}{\partial y}$ and find the value of $\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2$.	10.	CO2
Q12 (B)	Obtain a half range cosine series for $f(x) = \begin{cases} kx, & 0 \leq x \leq l/2 \\ k(l-x), & l/2 < x \leq l \end{cases}$	10	CO4
OR			
Q12 (B)	Find the Fourier series expansion of $f(x) = 2x - x^2, 0 < x < 3$ and hence find the value of $1 - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = ?$	10	CO4


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Name of the School <small>(Please tick, symbol is given)</small>	:	SOE	☐	SOCS		SOP	
Programme	:	B. Tech. ECE+EE					
Semester	:	I					
Name of the Course	:	Mathematics-I					
Course Code	:	MATH-1009					
Name of Question Paper Setter	:	Pankaj Kumar Mishra					
Employee Code	:	40000516					
Mobile & Extension	:	9897618899					
Note: Please mention additional Stationery to be provided, during examination such as Table/Graph Sheet etc. else mention "NOT APPLICABLE": NOT APPLICABLE							
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SECTION A

S. No.		Marks	CO
Q1	Determine the rank of matrix $\begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$.	4	CO1
Q2	Find the Eigen values and Eigen vectors of the matrix $\begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$.	4	CO1
Q3	Evaluate $\int_0^5 \int_0^{x^2} x(x^2+y^2) dA$, where dA indicates small area in xy -plane.	4	CO3
Q4	Prove $b_n = \frac{1}{\pi} \int_0^{2\pi} f(x) \cdot \sin nx dx$.	4	CO4
Q5	Find the Fourier coefficient b_n for $f(x) = \sqrt{1 - \cos x}$, $0 < x < 2\pi$	4	CO4

SECTION B

Q6	Find the inverse of matrix $\begin{bmatrix} 1 & 1 & 3 \\ 1 & 3 & -3 \\ -2 & -4 & -4 \end{bmatrix}$ using Cayley Hamilton Theorem, also convert the expression $A^5 - 20A^3 + 8A^2 + 2A + 5I$ into linear equation.	8	CO1
Q7	Evaluate $\iiint_R (x^2 + y^2 + z^2) dx dy dz$ where R denotes the region bounded by $x=0, y=0, z=0$ and $x+y+z=a, a>0$.	8	CO3

Q8	Evaluate $\iint_D xy\sqrt{(1-x-y)} dx dy$ where D is the region bounded by $x=0$, $y=0$ and $x+y=1$ using the transformation $x+y=u$, $y=uv$.	8	CO3
Q9	Change the order of integration $\int_0^1 \int_x^{\sqrt{2-x^2}} \frac{x}{\sqrt{(x^2+y^2)}} dy dx$ and hence evaluate	8	CO3
Q10	If $u=x^2-y^2$, $v=2xy$ and $x=r \cdot \cos \theta$, $y=r \cdot \sin \theta$ find Jacobean of (r, θ) with respect to (u, v) .	8	CO2
SECTION-C			
Q11 (A)	Prove that $\beta(m, 1/2) = 2^{2m-1} \beta(m, m)$.	10	CO2
Q11 (B)	Find the Fourier series of $f(t) = \begin{cases} -1, & -\pi < t < \pi/2 \\ 0, & -\pi/2 < t < \pi/2 \\ 1, & \pi/2 < t < \pi \end{cases}$	10	CO4
Q12 (A)	Find the equation of the tangent plane and normal line to the following surface $x^2+2y^2+3z^2=12$ at $(1, 2, -1)$.	10	CO2
OR			
Q12 (A)	If $u = \sin^{-1} \left(\frac{x+2y+3z}{\sqrt{x^8+y^8+z^8}} \right)$ then find the value of $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z}$.	10	CO2
Q12 (B)	Obtain the Fourier cosine series for $f(x) = \begin{cases} kx, & 0 \leq x \leq l/2 \\ k(l-x), & l/2 \leq x \leq l \end{cases}$, also deduce the sum of the series	10	CO4
OR			
Q12 (B)	Expand $f(x) = e^{-x}$ as a Fourier Series in the interval $(-l, l)$.	10	CO4