

Name:	
Enrolment No:	

UNIVERSITY OF PETROLEUM AND ENERGY STUDIES
End Semester Examination, December-22

Course: Mathematical Economics-I
Program: BA, Economics (Hons.)
Time: 03 Hours

Semester: III
Course code: ECON2026
Max. Marks: 100

SECTION A

1. Each Question will carry 2 Marks
2. Instruction: Select the correct answer(s)

		CO
Q1	<p>Find the domains of the functions defined by the following equations:</p> <p>a. $y = \sqrt{5 - x}$ b. $y = \frac{2x-1}{x^2-x}$ c. $y = \sqrt{\frac{x-1}{(x-2)(x+3)}}$ d. $y = \frac{3x+6}{x-2}$ e. $y = \frac{3x+6}{x-2}$ f. $y = \frac{1}{x+3}$ g. $y = \sqrt{2x+4}$ h. $y = \sqrt{x}$ i. $y = 1 - \sqrt{x+2}$ j. $y = \sqrt{5-x}$</p>	CO1

SECTION B

1. Each question will carry 5 marks
2. Instruction: Write short / brief notes

Q11.	<p>Find the equilibrium price and quantity for the following</p> <p>a. $D = 75 - 3P, S = -20 + 2P$ b. $D = 100 - 0.5P, S = -10 + 0.5P$</p>	CO2
Q12.	<p>Compute the following limits:</p> <p>a. $\lim_{x \rightarrow 2} (x^2 + 3x - 5)$ b. $\lim_{y \rightarrow -3} (1/y + 8)$</p>	CO2
Q13.	<p>Find the derivative of the following function</p> $y = \sqrt{x + \sqrt{x + \sqrt{x}}}$	CO2
Q14.	<p>Find $\frac{d^2y}{dx^2}$ when $y = x^a + x^{-a}$</p>	CO2

SECTION-C

1. Each Question carries 10 Marks.
2. Instruction: Write long answer

Q 15.	<p>For the following equations, find dy/dx by implicit differentiation:</p>	CO3
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	<ul style="list-style-type: none"> a. $xy = 1$ b. $x - y + 3xy = 2$ c. $y^6 = x^5$ d. $2x^2 + 6xy + y^2 = 18$ 	
Q16.	<p>Find the extreme value (s) of the following functions, and determine whether they are maxima or minima:</p> <ul style="list-style-type: none"> a. $z = x^2 + xy + 2y^2 + 3$ b. $z = -x^2 - y^2 + 6x + 2y$ 	CO3
Q17.	<p>Given $U = (X + 2) \cdot (y + 1)$ and $P_x = 4, P_y = 6$ and $M = 130$:</p> <ul style="list-style-type: none"> a. Write the Lagrangian function. b. Find the optimal levels of purchase x^* and y^*? c. Is the second-order sufficient condition for maximum satisfied? 	CO3
SECTION-D		
<p>1. Each Question carries 15 Marks. 2. Instruction: Write long answer</p>		
Q18	<p>Solve the following system of equations using appropriate theorem of Matrix Inversion:</p> <ul style="list-style-type: none"> a. $2x - 3y = 3, 3x - 4y = 5$ b. $2x - 3y = 8, 3x - 4y = 11$ c. $2x - 3y = 0, 3x - 4y = 0$ 	CO4
Q19	<p>Let the <i>IS</i> equation be</p> $Y = \frac{A}{1-b} - \frac{g}{1-b}i$ <p>Where $1 - b$ is the marginal propensity to save, g is investment sensitivity to interest rates, and A is an aggregate of exogenous variables. Let the <i>LM</i> equation be</p> $Y = \frac{M_0}{k} + \frac{l}{k}i$ <p>Where k and l are income and interest sensitivity of money demand, respectively, and M_0 is the real money balances.</p> <p>If $b = 0.7, g = 100, A = 252, k = 0.25, l = 200, \text{ and } M_0 = 176, \text{ then}$</p> <ul style="list-style-type: none"> a. Write the <i>IS - LM</i> system in matrix form. b. Solve for Y and i by matrix inversion. 	CO4